

# *Thesis Seminar*

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*Thursday, April 4, 2019  
1 pm in HH-3017*

*Graded modules over the Lie algebra  $\mathfrak{sl}_2(\mathbb{C})$*

**Abstract:** In this talk I will introduce some results from my future thesis. I will talk about the graded module over the Lie algebra  $\mathfrak{sl}_2(\mathbb{C})$ . First I will discuss the gradings of the weight  $\mathfrak{sl}_2(\mathbb{C})$ -modules. Then I will explain the gradings of the torsion-free  $\mathfrak{sl}_2(\mathbb{C})$ -modules of rank 1. This work has been published in a paper joint with Yuri Bahturin and Mikhail Kotchetov. Then I will focus on some new results about the torsion-free  $\mathfrak{sl}_2(\mathbb{C})$ -module of rank 2. I construct a new family of torsion-free  $\mathbb{Z}_2^2$ -graded modules of rank 2. I will show that “almost all” of these modules are simple. The remaining, reducible, modules in this family contain a unique maximal proper submodule, which is graded simple. Moreover, I will mention a general result about  $\mathbb{Z}$ -gradings of the simple torsion-free  $\mathfrak{sl}_2(\mathbb{C})$ -module of finite rank. This is joint work with Yuri Bahturin.