

# *Graduate Seminar in Mathematics*

*Speaker*

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1-2pm, HH-3017*

*A Halfway to the Pólya-Szegő Conjecture for Electrical Capacitance*

**Abstract:** Via a new  $(1,n)$   $p$ -isocapacitary inequality for the surface-area in  $\mathbb{R}^{n \geq 3}$  this note shows that  $\text{cap}_2(\Omega, \mathbb{R}^3) \geq (3,2) \sqrt{\pi} \sqrt{\text{area}(\Omega, \mathbb{R}^3)}$  holds for any bounded and convex set  $\Omega \subset \mathbb{R}^3$ . Whenever  $(3/2) \sqrt{\pi}$  (in the open interval  $(4/\sqrt{\pi}, 4\sqrt{2/\pi})$ ) is replaced by either  $4\sqrt{2/\pi}$  or  $4/\sqrt{\pi}$ , the induced inequality becomes either the Pólya-Szegő conjecture or the Pólya-Szegő inequality for the electrical capacitance.