

1. Wadley (1946 *Journal of Economic Entomology* 38:651) reported percentage of flower buds attacked by boll weevils in 16 plots each treated with a different type of arsenical insecticide. The experiment was repeated in 5 different fields for a total of 80 plots. Are some insecticides more effective than others, after controlling for differences in location?

Define variables in a tabular format, as in the box. [3]

scale = nominal, ordinal, or cardinal
cardinal = interval or ratio scale.

A. name	symbol	scale
% Buds	%B	cardinal
IType	IT	nominal
Field	F	nominal

Using the symbols, write a general linear model relating the response variable to explanatory variable(s) and interaction terms (if appropriate).

List degrees of freedom beneath each term in the model,

Assume 1 measure of flower bud % per plot.

60df cannot estimate

$$\begin{aligned} \text{df= } \frac{\%B}{79} &= \frac{\beta_0 + \beta_{IT} \cdot IT + \beta_F \cdot F + \beta_{IT \cdot F} \cdot IT \cdot F}{15 + 4} + \epsilon & [3] \\ & & + 60 & [4] \end{aligned}$$

State the name of the analysis, from the following list. [1]

- t-test, one-way ANOVA, two-way ANOVA,
- three-way ANOVA
- paired comparisons, randomized blocks,
- hierarchical (nested) ANOVA
- regression, multiple regression,
- ANCOVA (at least one nominal and at least 1 cardinal scale explanatory variable)
- none of the above.

Using the same symbols, write a general linear model given 2 measurements per plot. List degrees of freedom beneath each term in the model.

$$\begin{aligned} \text{df= } \frac{\%B}{160-1} &= \frac{\beta_0 + \beta_{IT} \cdot IT + \beta_F \cdot F + \beta_{IT \cdot F} \cdot IT \cdot F}{15 + 4 + 60} + \epsilon & [4] \\ & & + 79 & [5] \\ & & 80 & \end{aligned}$$

2. J. Neter, W. Wasserman, and M.H. Kutner 1985 *Applied Linear Statistical Models* reported muscle mass in 8 women, in the 43-58 year age range.

Does muscle mass M (kg) decrease with age A in this range? (H_0 testing)

The question can also be phrased as:

How good is the evidence for a decrease in muscle mass with age in this range?

Using the symbols above write a GLM to address this question.

$$\frac{M}{\text{kg}} = \frac{\beta_0}{\text{kg}} + \frac{\beta_A}{\frac{\text{kg}}{\text{yr}}} \cdot A + \varepsilon \quad [2]$$

Show units below each symbol in your GLM. [5]

Write the null hypothesis.

$$H_0 \quad \beta_A = 0 \quad \text{or} \quad \text{var}(\beta_A) = 0 \quad \text{or} \quad \text{var}(\beta_A \cdot A) = 0 \quad [1]$$

Complete the ANOVA table [6]

age	Source	df	SS	MS	F	p
43-58	regr	1	70.64	70.64	10.228	0.02
	residual	6	41.44	6.91		
	total	7	112.08			

Calculate the explained variance $R^2 = \frac{70.64}{112.08} = 0.63$ [1]

Calculate the likelihood ratio. $LR = \frac{1}{(1 - 0.63)^{-8/2}} = 54$ [1]

Declare a decision about H_0 against a 5% tolerance for statistical significance. [1]

H_0 : Reject the null at $\alpha = 5\%$

Choose one of the following methods of reporting statistical conclusions. (circle it). [1]

Report the likelihood ratio as relative evidence:

“change with age was () times more likely than no change”

Report Type I error with a decision.

“the null hypothesis was (or was not) rejected at $\alpha = 5\%$.”

Give a reason for your choice. [2]

3. Cochran and Cox (1957 *Experimental Designs* Table 4.4) reported the breaking strength of cotton fibers from 5 blocks, each with 5 plots treated with a different level of potash (36, 54, 72, 108, or 144 lbs K₂O / acre). Does cotton property (breaking strength) depend on level of potash, controlled for soil pH ?

Define variables in a tabular format, as in the box. [3]

scale = nominal, ordinal, or cardinal
cardinal = interval or ratio scale.

A. name	symbol	scale
Br Strength	Bstr	cardinal
Potash	pP	nominal
pH	pH	cardinal
[Block]	B	nominal

Using the symbols, write a general linear model relating the response variable to explanatory variables and interaction term.

$$BS_{tr} = \beta_0 + \beta_p \cdot P + \beta_{pH} \cdot pH + \beta_{p \cdot pH} \cdot P \cdot pH + \epsilon \quad [4]$$

Assume 2 measures of breaking strength and one measure of pH per plot.

Show how to calculate the total degrees of freedom. $2 \times 5 \times 5 - 1 = 49$ [1]

Complete the source column. [1]

Complete the df column of the ANOVA table. [5]

C. source	df
p	4
pH	1
p × pH	4
residual	40
total	49

State the name of the analysis, from the following list.

- t-test, one-way ANOVA, two-way ANOVA, three-way ANOVA
- paired comparisons, randomized blocks, hierarchical (nested) ANOVA
- regression, multiple regression,
- ANCOVA (at least one nominal and at least 1 cardinal scale explanatory variable)
- none of the above.

[1]

p	4
pH	1
B	4
p × pH	4
res	36
total	49

p	4
pH	1
B	4
p × B	16
res	24
total	49