

1. The expected number of events  $k$  in area  $A$ , if events are rare and random, follows a Poisson distribution. The expected frequency of events  $\Pr(X=k)$  for a Poisson distribution is calculated as

$$\Pr(X=k) = e^{-\mu} \mu^k / k! \quad k = 0,1,2,3 \text{ etc}$$

$$\Pr(X=0) = e^{-2} 2^0 / 0! = 0.135$$

where  $\mu = \lambda A$ ,  
 $e$  is approximately 2.71828, any number to the zero power is 1,  
 and  $k!$  ( $k$  factorial) is  $0! = 1, 1! = 1, 2! = 2*1, 3! = 3*2*1, \text{ etc.}$

If a laboratory population of bacteria grows at a density of  $\lambda = 0.02/\text{cm}^2$ , what is the probability of finding no colonies  $\Pr(X=0)$  in an area of  $A = 100 \text{ cm}^2$  ?

Beneath the equation, write the equation with the numbers you plan to use. [1]

Compute the probability of finding no colonies  $\Pr(X=0)$  if  $A = 100 \text{ cm}^2$  0.135 [1]

2. Construct the frequency distribution  $F(Y=k)$  and the cumulative relative frequency distribution  $RF(Y \leq k)$  from the cumulative frequency distribution  $F(Y \leq k)$  of mites found on 589 chironomid flies, where the outcomes are  $k =$  number of mites per chironomid fly (from Sokal and Rohlf 1995, Box 5.6).

$k$	$F(Y=k)$	$F(Y \leq k)$	$RF(Y \leq k)$	
0	<u>442</u>	442	<u>442/589 = 0.75</u>	[2]
1	<u>91</u>	533	<u>0.905</u>	[2]
2 or more	<u>56</u>	589	<u>1.00</u>	[2]

3. If the probability of an outcome is some percentage  $p$ , then the odds in favour of the outcome are defined as  $\text{Odds} = p/q$  where  $q = 1 - p$ . The odds against that outcome are thus  $q/p$ . Odds are expressed relative to a value of 1.  
 Read the expression (Odds = 4: 1) as "odds are 4 to 1."

If the probability of finding an uninfected chironomid had been 30%,  
 what are the odds of finding an uninfected chironomid ? 0.43:1 [1]

what are the odds of finding an infected chironomid ? 2.33:1 [1]