

1. The general linear equation is a compact summary of many forms of parametric statistical analysis. The equation has the form:

Response = Explanatory + residual

$$Y = \beta_0 + \beta X + \epsilon$$

The systematic part of the model (treatment or explanatory component) can consist of several terms ($\beta_1 X_1 \beta_2 X_2$ etc) composed of parameters β and variables X . Write a general linear equation for each of the following designs.

nested ANOVA

t-test

Regression

Analysis of Covariance

Underline all interval or ratio scale variables. Circle all classification (nominal scale) variables. Don't forget to underline or circle both explanatory and response variables.

2. An entomologist observes the number of scale insects (n_t) on a tree in 9 successive days. Assuming an invariant mortality rate of $m = 0.2 \text{ day}^{-1}$ the expected number of scale insects (\hat{n}_t) is

$$\hat{n}_t = n_{t=0} e^{-mt}$$

Which column shows the residuals (difference between observed and expected) from this model ? _____

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MTB > print c1-c7
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ROW	t=days	n_t	\hat{n}_t	C4	C5	C6
1	0	100	100.000	1.00000	0.00000	-0.04136
2	4	46	44.933	1.02375	1.06710	0.99750
3	5	38	36.788	1.03295	1.21206	1.21098
4	6	32	30.119	1.06244	1.88058	1.84663
5	7	23	24.660	0.93270	-1.65970	-1.70339
6	8	18	20.190	0.89155	-2.18965	-2.25062
7	9	15	16.530	0.90745	-1.52989	-1.55144

Based on the residuals does mortality appear to be invariant over time ? _____

State why or why not.

3. According to Schreck (1982 p 200 in Air Pollution--Physiological Effects) the Stokes number ST can be used to predict the tendency for deposition of particles in lung airways:

$$St = \frac{\rho d^2 v}{18 \text{ MU } R}$$

where ρ is the density of particles (gram/litre),
 d is the diameter of particles ($\mu\text{m} = 10^{-6}\text{m}$),
 v is the velocity of particles ($\mu\text{m}/\text{second}$),
 MU is absolute viscosity of air ($\text{g m}^{-1} \text{second}^{-1}$)
 and R is the airway radius (cm).

Schreck (1982 p 207) reports that deposition in volunteer subjects varied in accordance with an anatomical Stokes number ST^*

$$St^* = \frac{4 d^2 F}{18 \text{ MU } \pi (\text{BDS})^3}$$

where F is flow rate (litres/minute) and
 BDS is bronchial deposition size ($\text{cm} = 10^{-2}\text{m}$).

Which Stokes number (St or ST^*) does not have dimensions (*i.e.* is correct) ? _____

Justify your answer by showing the dimensions for the incorrect Stokes Number
 Show dimensions as exponents for M L T (Mass, Length, Time)

4. One goal of this course in quantitative methods was to increase your skill in moving among 3 forms of generalization: verbal, graphical, and formal models. Draw a picture showing the relation between data (or quantities) and these 3 forms of generalization.

Circle the forms of generalization that you would use in presenting your research in a paper or thesis.

Redraw the diagram and circle the form of generalization you would use in presenting your results to a newspaper reporter.

5. List two ways of judging whether a set of residuals are normally distributed.

List two solutions to the problem of non-normal residuals.
(List the better solution first)

Justify your choice of which solution to list first.

6. An ethologist records the turning movements of a planarian worm as follows:
R L L R L L L R R L R R L L L R R L L R R

The number of left turns is $L =$ _____

If turning is random, what is the expected number of R(ight) turns immediately after a L(eft) turn ? _____

What is the observed number of R turns immediately after an L turn? _____

State a null Hypothesis H_0 : _____

H_A : _____

Describe a randomization test with this data, to evaluate whether planarian worms turn at random.

7. A geneticist (Sewall Wright 1968 p 203) reported the mean weights (W = grams) of guinea pigs.

Three analyses of the data are attached (A, B, and C) below, as Minitab outfiles.

Calculate the observed difference in mean weight between the two strains

$D =$ _____ grams

You have been asked to determine whether this difference is statistically significant. Using the response variable W , write a General Linear Model for each of the 3 ANOVA tables (analyses).

Analysis A _____

Analysis B _____

Analysis C _____

Underline all interval or ratio scale variables. Circle all classification (nominal scale) variables. Don't forget to underline or circle both explanatory and response variables.

Which analysis is better A or B ? _____

Why ?

Is analysis C an improvement over either A or B ? _____

Why or why not ?

8. Xenon lighting is less expensive than other electrical lighting, but emits light within a narrow range of wavelengths, compared to other artificial lighting. You have been asked to determine whether xenon lighting reduces growth rates of cucumbers in a greenhouse, compared to other sources of lighting.

Name your response quantity (including symbols, units, and procedural statement).

Name at least two explanatory variables that should be included in your investigation (be sure to write a symbol and procedural statement for each named explanatory variable).

Write a general linear model (GLM) to use in testing the effects of lighting on cucumber growth.

State a pair of hypotheses (H_0/H_A) for each term in your model.

Construct an ANOVA table (Source and df columns only) for your analysis. To do this you will need to decide how many observations to make, as well as how many levels to use for each classification variable.

MTB > print c1-c6

ROW	year	strain13	strain35	weight	strain	yr
1	1916	190.7	195.4	190.7	13	1916
2	1917	206.3	206.7	206.3	13	1917
3	1918	239.3	223.0	239.3	13	1918
4	1919	240.4	227.2	240.4	13	1919
5	1920	259.0	232.4	259.0	13	1920
6	1921	228.6	207.1	228.6	13	1921
7	1922	234.2	230.3	234.2	13	1922
8	1923	256.3	245.9	256.3	13	1923
9	1924	257.0	244.8	257.0	13	1924
10				195.4	35	1916
11				206.7	35	1917
12				223.0	35	1918
13				227.2	35	1919
14				232.4	35	1920
15				207.1	35	1921
16				230.3	35	1922
17				245.9	35	1923
18				244.8	35	1924

MTB > anova 'weight' = 'strain' ANALYSIS A

Factor	Type	Levels	Values
strain	fixed	2	13 35

Analysis of Variance for weight

Source	DF	SS	MS	F	P
strain	1	544.5	544.5	1.28	0.275
Error	16	6823.4	426.5		
Total	17	7367.9	433.4		

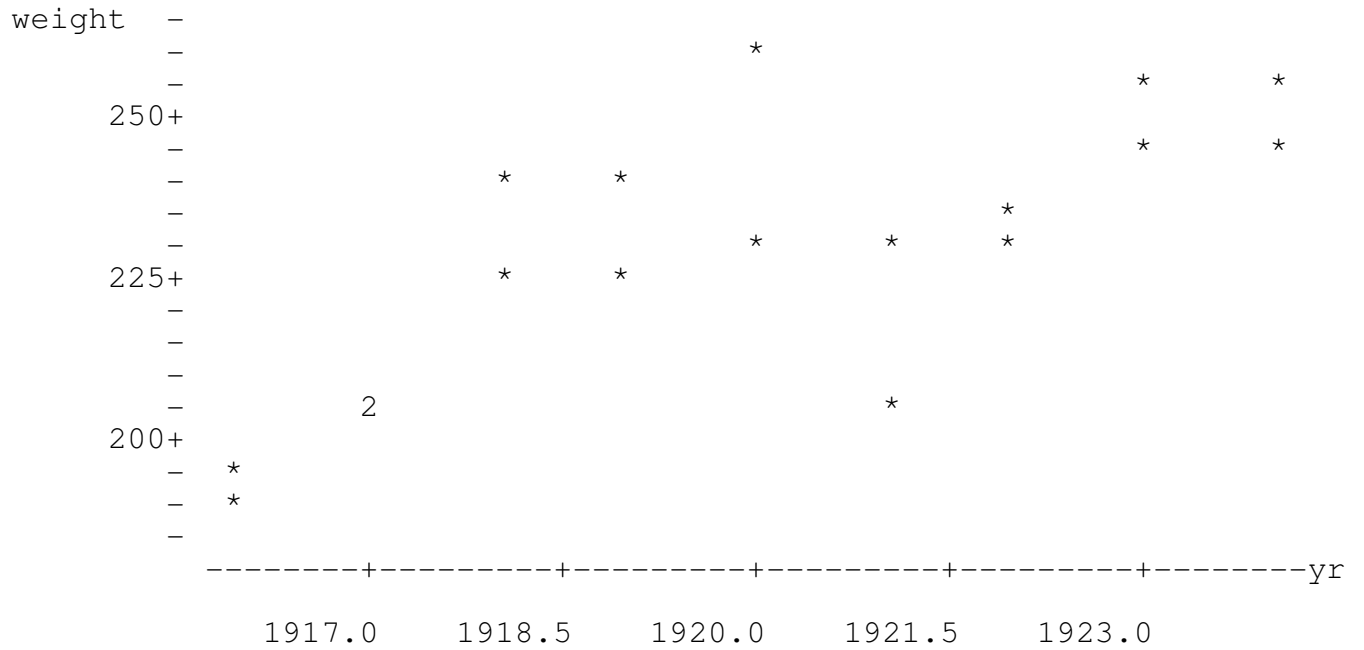
MTB > anova 'weight' = 'strain' 'yr' ANALYSIS B

Factor	Type	Levels	Values
strain	fixed	2	13 35
yr	fixed	9	1916 1917 1918 1919 1920 1921 1922 1923 1924

Analysis of Variance for weight

Source	DF	SS	MS	F	P
strain	1	544.5	544.50	10.69	0.011
yr	8	6415.8	801.98	15.74	0.000
Error	8	407.6	50.95		
Total	17	7367.9	433.41		

MTB > plot 'weight' by 'yr'



MTB > ancova weight = strain; ANALYSIS C
SUBC> covariates yr.

Factor	Levels	Values
strain	2	13 35

Analysis of Covariance for weight

Source	DF	ADJ SS	MS	F	P
Covariates	1	4117.2	4117.2	22.82	0.000
strain	1	544.5	544.5	3.02	0.103
Error	15	2706.2	180.4		
Total	17	7367.9	433.4		

Covariate	Coeff	Stdev	t-value	P
yr	5.858	1.23	4.777	0.000

MTB > stop

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