

1. The Michaelis–Menten enzyme kinetics model (1913 *Biochem Z* 49: 333–369) is named after German biochemist Leonor Michaelis and Canadian physician Maud Menten. Yu and Rappaport (1997 *Environ Health Perspectives* 105 : 496–503) show that the Michaelis Menten model describes the clearance rate ( $k$ ) of insoluble dust particles from lungs as a function of the maximum rate ( $k_{max}$ ), the particulate burden ( $m$ ), and the particulate burden ( $m_{half}$ ) at which  $k$  is half of  $k_{max}$ .

$$k = \frac{k_{max} \cdot m_{half}}{m + m_{half}} \qquad k = k_{max} \left( \frac{m_{half}}{m + m_{half}} \right)$$

The parameter  $m_{half}$  and the variable  $m$  have units of milligrams (mg),  $k$  has units of %/day

a. Show units for the ratio in parentheses \_\_\_\_\_ and for  $k_{max}$  \_\_\_\_\_ [1+1]

b. Explain your answer for units of  $k_{max}$  [2]

c. Does the ratio in parentheses increase or decrease as lung burden  $m$  increases?

Write your answer here \_\_\_\_\_ [no mark]

d. Given  $m_{half} = 2.49$  mg for diesel exhaust particles (DEP) and  $k_{max} = 0.009$ /day for experimental rats, calculate the expected clearance rate at

$$m = 0.5 \text{ mg} \qquad E(k) = \underline{\hspace{2cm}} [1]$$

$$m = 5 \text{ mg.} \qquad E(k) = \underline{\hspace{2cm}} [1]$$

d. Show your calculations, with units, for 0.5 mg [2]

e. Does the expected clearance  $E(k)$  change in the direction you expected, with increase in lung burden  $m$  ? [no mark]

2. Using the expected value  $E(k)$  at a burden of  $m = 0.5$  mg, complete a data equation for an observed value of  $k = 0.008$

$$\begin{array}{rclcl} k & = & E(k) & + & \text{residual} \\ \underline{\hspace{1cm}} & = & \underline{\hspace{1cm}} & + & \underline{\hspace{1cm}} \end{array} \qquad [3]$$