Model Based Statistics in Biology.Part IV. The General Linear Model. Multiple Explanatory Variables.Chapter 13.5 Repeated MeasuresTo be completed

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ReCap.	Part I (Chapters 1,2,3,4), Part II (Ch 5, 6, 7)		
ReCap	Part III (Ch 9, 10, 11)		
ReCap	Multiple Regression (Ch 12)	Chl	3.xls
13.1 Fix	ed Effects ANOVA (no interactive effects)		
13.2 Fix	ed Effects ANOVA (interactive effects)		
13.3 Fix	ed*Random Effects (Paired t-test)		
13.4 Fix	ed*Random Effects (Randomized Block)		
13.5 Seq	uential within Random (Repeated Measures)		
13.6 Nes	sted Random Effects (Hierarchical ANOVA)		
13.7 Rar	ndom within Fixed (problem of confounding)		
13.8 Mo	re Than Two Factors (to be written)		

on chalk board

ReCap Part I (Chapters 1,2,3,4) Quantitative reasoning is based on models, including statistical analysis based on models.

ReCap Part II (Chapters 5,6,7)

<u>Hypothesis testing</u> uses the logic of the null hypothesis to declare a decision.

Estimation is concerned with the specific value of an unknown population parameter.

ReCap (Ch 9, 10,11) The General Linear Model with a single explanatory variable.

ReCap (Ch 12) GLM with more than one regression variable (multiple regression)

ReCap (Ch 13) GLM with more than one categorical variable (ANOVA).

Two fixed factors (Ch 13.1, Ch13.2)

Today: Special case of two factor ANOVA: Repeated Measures

One fixed and one random factor (Paired t-test, Randomized block)

Wrap-up.

Introduction. A very common design is to make repeated measurements of the response variable within a unit of a random factor. Repeated measures can be longitudinal-repeated measures on the same individual assigned to one level of a fixed factor. Repeated measures can be cross-sectional. That is, repeated measures on an individual, with re-assignment of the individual to another level of the fixed factor. This is called a cross-over design. The major advantage of this design is that variation among units can be removed from the analysis, allowing a more sensitive test of the fixed factor of interest. Adding measurements within a unit costs less than adding units. The repeated measures design thus resembles the randomized blocks design, having the same motivation–a more sensitive analysis with lower Type II error (erroneously failing to reject the null hypothesis). The concern is that repeated measurements in time (or within a unit in space) are autocorrelated—they cannot be taken as independent estimates of the response variable.

Some definitions.

A unit (one level of a random factor) is measured repeatedly.
eatments applied in random order to each subject.
Only one treatment to a unit, measured repeatedly.
ze of fish in a tank on several occasions to obtain growth rate.
atments assigned randomly to adjacent subplots (2 or more).
plied in random order, if possible, to eliminate carry-over.
A factor is applied to units that can be matched by a random
factor, such as propinquity in time or space.
ed out in 3 different labs (blocks).
ed out on 4 different occasions (blocks).
Two levels of a factor within a unit (repeated measures), or in
pair of units matched according to some random factor
(randomized blocks).

The general linear model will have a fixed factor of interest, and a random factor (defined unit or random block). Interaction terms cannot be estimated because fixed and random factors do not pass the cross test.

Example Data from

1. Construct model

Verbal model.

Graphical model. Plot of

Write GLM: $T = \$_o + \$_U \And_U + \$_E \And_E + \$_{D \times S} \And_D \And_S + \text{residual}$ S&R95 $T_{::i} = \therefore + A_i + \$_i + (A \circledast)_{:i} + \ldots$ Formal Model

2. Execute analysis.

Place data in model format:

Column labelled L, with response variable Column labelled X_U , with explanatory variable X_U = Column labelled X_E with

Code model statement in statistical package according to the GLM

 $L = \$_{o} + \$_{U} \And X_{U} + \$_{E} X_{E} + ,$

```
MTB > anova 'wlngth' = 'XU' 'XE';
SUBC> fits c4;
SUBC> residuals c5.
```

Here are the parameters of the model: the overall mean ($_{o}$), the mean for... and the fitted values -- the mean for each fly ($_{o} + _{U E}$).

$$\hat{\boldsymbol{\beta}}_{o} =$$
mean(L) = 24^{! 1} @

$$\hat{\beta}_{o} + \hat{\beta}_{E} = \max(L_{cage=II}) \\ \max(L_{cage=III}) \\ \max(L_{cage=III})$$

The residuals for each measurement are computed from the means.

- **3. Evaluate the model** Plot residuals versus fitted values.
- a. No line fitted in model, so skip evaluation of straight line assumption.
- b. Homogeneity of residuals.
- c. If n small, evaluate assumptions for chisquare (t, F) distributions.

n = 24

<u>Homogeneous</u>? <u>Sum(res) = 0</u>? Independent?

Normal?

- 4. State population and whether sample is representative.
- 5. Decide on mode of inference. Is hypothesis testing appropriate?
- 6. State H_A H_o pairs, test statistic, distribution, tolerance for Type I error.

Are there more specific hypotheses about parameters? NoState test statisticF-ratioDistribution of test statisticF-distributionTolerance for Type I error5% (conventional level)

7. ANOVA table: set up.

GLM: Y Source: tota	= \$ _o		$_{\rm U}X_{\rm U}$ + $\$_{\rm E}X_{\rm H}$ Init Effective	$E_{\rm E}$ + res ect res	
Source Unit Effect <u>Error</u> Total	df	SS	MS	F	> p

ANOVA. Calculate df, partition according to model.

GLM: Source:	Y = total = 24 ! 1 =	\$ ₀ +	$U_U X_U + U_U X_U + U_U X_U + 3! 1 +$	$E_E X_E + Effect +$	res res + 12
Source Unit Effect <u>Error</u> Total	$\begin{array}{cc} df & SS \\ 2 \\ 9 \\ \underline{12} \\ 23 \end{array}$	MS F	> p		

7. ANOVA. Calculate variance, partition according to model.

Calculate $SS_{total} = 23* Var(L) = 23*104.43 = 2401.98$

Here is the partitioning of the SS_{total} produced by any statistical package.

GLM:	Y	=	\$ _o	+	$U_U +$	$E_E X_E$	+	res
	2401	.97=			665.68 +	1720.68	+	15.62

Source	df	SS	MS	F	> p	
Unit	2	665.68			-	
Effect	9	1720.68				
Error	12	15.62				
Total	23	2401.97				

Table SS, MS, F-ratio. Calculate MS = SS/df

Source	df	SS	MS	F	> p	
Unit	2	665.68	332.84		_	
Effect	9	1720.68	191.19			
Error	12	15.62	1.3017			
Total	23	2401.97				

Calculate F ratios.

Calculate Type I error from F-distribution.

8. Decide whether to recompute p-value.

9. Declare decision about terms.

10. Report and interpret parameters of biological interest.