

## Derivation of Hardy-Weinberg Ratios for dioecious organisms

Let individuals with genotypes **AA**, **AB**, & **BB** be distributed as  $p^2 : 2pq : q^2$

Let ratios in **females** & **males** be equal.

### I. Proportion of total offspring contributed by each type of mating

	$p^2$ 'AA'	$2pq$ 'AB'	$q^2$ 'BB'
$p^2$ 'AA'			
$2pq$ 'AB'			
$q^2$ 'BB'			

### II. Expected genotype ratios from each type of mating

	'AA'	'AB'	'BB'
'AA'			
'AB'			
'BB'			

### III. Expected proportions of genotypes produced by each type of mating: multiply proportions in (I) by expectations in (II)

	$p^2$ 'AA'	$2pq$ 'AB'	$q^2$ 'BB'
$p^2$ 'AA'			
$2pq$ 'AB'			
$q^2$ 'BB'			

Then, summing over genotypes

$$f(\mathbf{AA}) = p^4 + p^3q + p^3q + p^2q^2 = p^2$$

$$\begin{aligned} f(\mathbf{AB}) &= p^3q + p^2q^2 + p^3q + 2p^2q^2 + p^2q^2 + pq^3 \\ &= 2p^3q + 4p^2q^2 + 2pq^3 = 2pq \end{aligned}$$

$$f(\mathbf{BB}) = p^2q^2 + pq^3 + pq^3 + q^4 = q^2$$

**Conclusion:** random *matings* between *dioecious* organisms produce the same genotype ratios as random *union of gametes* in *monoecious* organisms